AP Test Question 2009
No Calculator Allowed

4) Let $R$ be the region in the first quadrant enclosed by the graphs of $y=2 x$ and $y=x^{2}$, as shown in the figure above.
a) Find the area of $R$.
b) The region $R$ is the base of a solid. For this solid, at each $x$ the cross section perpendicular to the $x$-axis has area $A(x)=\sin \left(\frac{\pi}{2} x\right)$. Find the volume of the solid.
c) Another solid has the same base $R$. For this solid, the cross sections perpendicular to the $x$-axis are squares. Write, but do not evaluate, an integral expression for the volume of the solid.

